

Projective Adaptive Resonance Theory Revisited with Applications to Clustering Influence Spread in Online Social Networks

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Abstract— We revisit the theory and applications of the Projective Adaptive Resonance Theory (PART) neural network architecture for clustering high dimensional data in low dimensional subspaces and nonlinear manifolds. We put a number of PhD theses, research publications and projects of the York University’s Laboratory for Industrial and Applied Mathematics (LIAM) in a coherent framework about information processing delay, high dimension data clustering, and nonlinear neural dynamics. The objective is to develop both mathematical foundation and effective techniques/tools for pattern recognition in high dimensional data.

Keywords— *projective clustering; nonlinear dynamics in processing high dimensional data; influence spread in online social network.*

I. INTRODUCTION

In a series of studies starting in the papers [1] [2] and the thesis [3], the Laboratory for Industrial and Applied Mathematics (LIAM) at York University (Toronto, Canada) has been developing a comprehensive framework about information processing delay, high dimension data clustering, and nonlinear neural dynamics. The objective is to develop both mathematical foundation and effective techniques/tools for pattern recognition in high dimensional data. Some of the earlier developments have been reported in the monograph [4] and the survey [5]. The survey also provided a heuristic description of the philosophy about how the modern nonlinear dynamic systems theory (invariant manifolds, domain attractions, global convergence, Lyapunov functions etc.) provides some theoretical principles based on recent biological evidences for novel neural network based clustering architectures to speed up information processing to assist decision making. Here, we briefly describe the current status (Section II) and then summarize the interdisciplinary nature (Section III) of a high dimensional data projective-clustering driven academic-industrial collaboration based on nonlinear dynamics and neural networks.

II. CURRENT STATUS

Under the framework “Projective Adaptive Resonance Theory” (PART), we developed a novel neural network architecture and algorithm to detect low dimensional patterns in a high dimensional data set. These are the patterns characterized by the so-called projective clusters, in nonlinear subspaces or nonlinear manifolds. PART has received much attention by data science researcher and

end-user community, and has formed the core data analytics tools of three Collaborative Research Development projects (CRD), funded by the Natural Science and Engineering Research Council of Canada (NSERC). In particular, the NSERC CRD project Enterprize Software for Data Analytics in collaboration with InferSystems Inc. is based on the application of PART to analyzing odd bidding behaviors in a real-time bidding auction; while the project An Online Integrated Health Risk Assessment Tool brings together a team of investigators with expertise for an interdisciplinary and multi-institutional collaboration to develop systematic analyses converging on a single number, modeled after the single-number Credit Score, to inform chronic disease decision making, both at the population and individual levels. These are also part of a newly funded NSERC Collaborative Research and Training Experience Program in Data Analytics & Visualization.

The PART algorithm has since been used in a number of applications. It was used to develop a powerful gene filtering and cancer diagnosis method in [6][7][8], which shows that “*the results have proven that PART was superior for gene screening*”. PART was also used for clustering neural spiking trains [9], ontology construction [10], stock associations [11], and information propagation in online social networks [12][13]. The PART algorithm has also been extended to deal with categorical data in the thesis [14].

The PART architecture is based on the well known ART developed by Carpenter and Grossberg, with a selective output signaling (SOS) mechanism to deal with the inherent sparsity in the full space of the data points in order to focus on dimensions where information can be found. The key feature of the PART network is a hidden layer of neurons which incorporates SOS to calculate the dissimilarity between the output of a given input neuron with the corresponding component of the template (statistical mean) of a candidate cluster neuron and to allow the signal to be transmitted to the cluster neuron only when the similarity measure is sufficiently large. *Recently discovered physiological properties* of the nervous system, the adaptability of transmission time delays and the signal losses that necessarily arises in the presence of transmission delay, enabled us to interpret SOS as a plausible mechanism from the self-organized adaptation of transmission delays driven by the aforementioned dissimilarity. The result is a

novel clustering network, termed PART-D, with physiological evidence from living neural network and rigorous mathematical proof of exceptional computational performance [15].

Such an adaptation can be regarded as a consequence of the Hebbian learning law, and the dynamic adaptation can be modeled by a nonlinear differential equation using dissimilarity driven delay in signal processing. This links to the PhD thesis [16], which proposed an alternative neural network formulation of the Fitts' law for the speed-accuracy trade-off of information processing, and its subsequent publications including [17][18][19][20]. When the delay adaptation rates are in certain ranges, we observe nonlinear oscillatory behaviors (clustering switching) and this oscillation slows down the convergence of the clustering algorithm. How to detect and prevent these oscillations is the focus of the thesis [21] the studies [22][23].

III. SUMMARY

In summary, there have been increasing physiological evidences to support the idea of projective clustering using neural networks with delay adaption, there has been some theoretical analysis to show why such a network architecture works well for high dimensional data, and there have been sufficient applications to illustrate PART clustering algorithms are efficient. An interdisciplinary approach for high dimensional data clustering clearly shows the potential to develop a dynamical system framework for pattern recognition in high dimensional data.

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